

Atmospheric Vectors

By utilizing vectors in Meteorology, information may be obtained About reported winds by performing vector addition and subtraction.

SCALAR & VECTOR QUANTITIES.

Scalar Quantity – Any physical quantity (temperature, density, or humidity) which only has a single numerical value (magnitude).

Distance: The measurement of the separation of 2 points. Units is meters (m).

Area (A): The measurement of a 2 dimensional surface. Units is meters squared (m^2)

Volume (V): The amount of space that an object occupies. Units is meters cubed (m^3)

Speed: Displacement per unit time. Units may be a variety, knots, mph, km

Density (ρ): The amount of mass per unit volume. Equation is $\rho = m/V$.

Where – ρ is density (greek letter “rho”)

m is the mass of the substance

V is the volume that it occupies

Measured in kg/m^3

SCALAR & VECTOR QUANTITIES.

Density (ρ): The amount of mass per unit volume. Equation is $\rho = m/V$.

Where - **ρ** is density (greek letter “rho”)

m is the mass of the substance

V is the volume that it occupies

Measured in kg/m^3

Relationships -

If the mass is doubled, what happens to density?

$$\uparrow \rho = \uparrow m / \dot{V}$$

$$\downarrow \rho = \downarrow m / \dot{V}$$

If the volume increases to 5 times the original values, what happens to density?

$$\downarrow \rho = \dot{m} / \uparrow V$$

$$\uparrow \rho = \downarrow m / \dot{V}$$

SCALAR & VECTOR QUANTITIES.

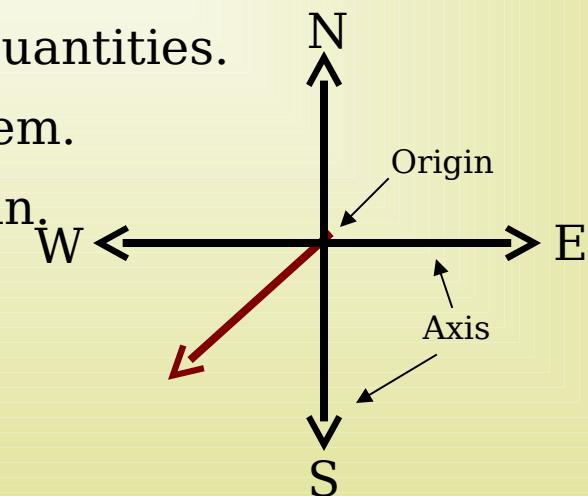
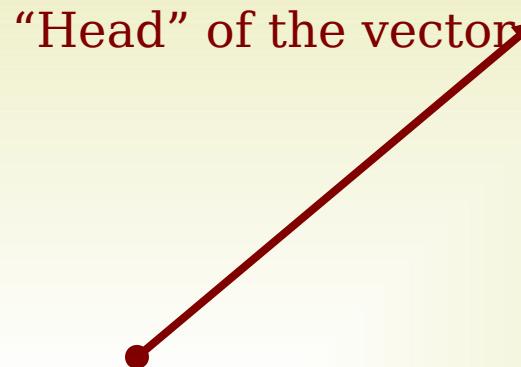
Vector: Any quantity which has both magnitude and direction.

Represented Mathematically:

27008 kts

Represented
Graphically:

- An arrow represents the vector.
- Arrow Length is proportional to the magnitude of the vector.
- Points in the direction the object is moving ("towards").
- A magnitude and direction describe vector quantities.
- Plotted on the Navigational Coordinate System.
- End point of the vector is plotted at the origin.



SCALAR & VECTOR QUANTITIES.

Examples of a Vector

Velocity (v) : Displacement per unit time in a particular direction.

Average Velocity (v): Displacement over some time interval.

Equation - $|v| = |\Delta x| / |\Delta t|$

Where - $|v|$ is average velocity
 $|\Delta x|$ is displacement
 $|\Delta t|$ is the time interval

Relationships -

If velocity increases,
what happens to displacement?

$$\uparrow v \Rightarrow \Delta x \bullet / \Delta t$$

If velocity decreases,
what happens to displacement?

$$\downarrow v \Rightarrow \Delta x \bullet / \Delta t$$

VECTOR OPERATIONS.

Vector Operations

Addition – Utilize graphical “head-to-tail” method

- Step #1 – Construct a x,y coordinate system.
- Step #2 – Select a scale and plot vector “A” to scale.
- Step #3 – Plot vector “B”, with proper orientation using another coordinate on the head of vector “A”.
- Step #4 – Draw the Resultant vector “R” from the origin of “A” to the head of the last vector plotted.

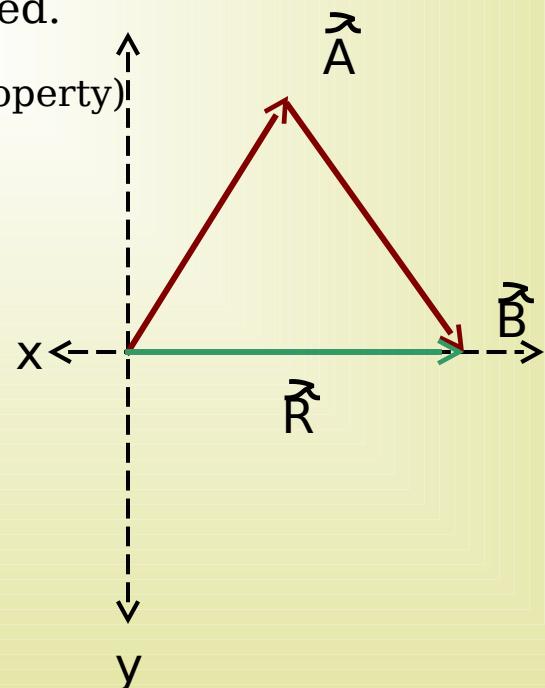
NOTE: The order of addition makes no difference (Cumulative Property)

$$(A + B = B + A)$$

Meteorological
Uses

- Resultant of Forces.

- Average Wind for a Layer.



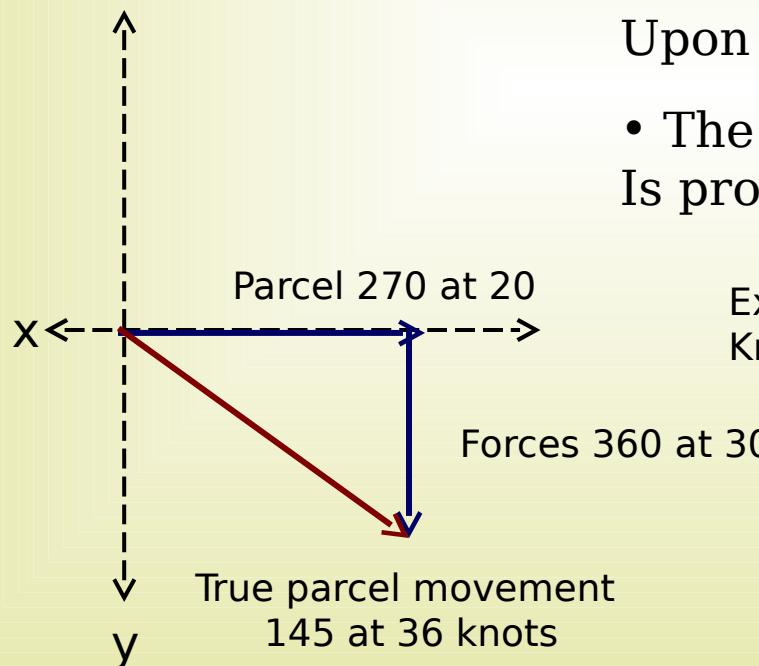
VECTOR OPERATIONS.

Vector Addition

Addition - Utilize graphical “head-to-tail” method.

Meteorological Uses - Resultant of Forces

- The direction of a parcel's movement can be found by the vector sum of all forces acting upon the parcel.
- The magnitude of change in the parcel's movement is proportional to the magnitude of the resultant force.



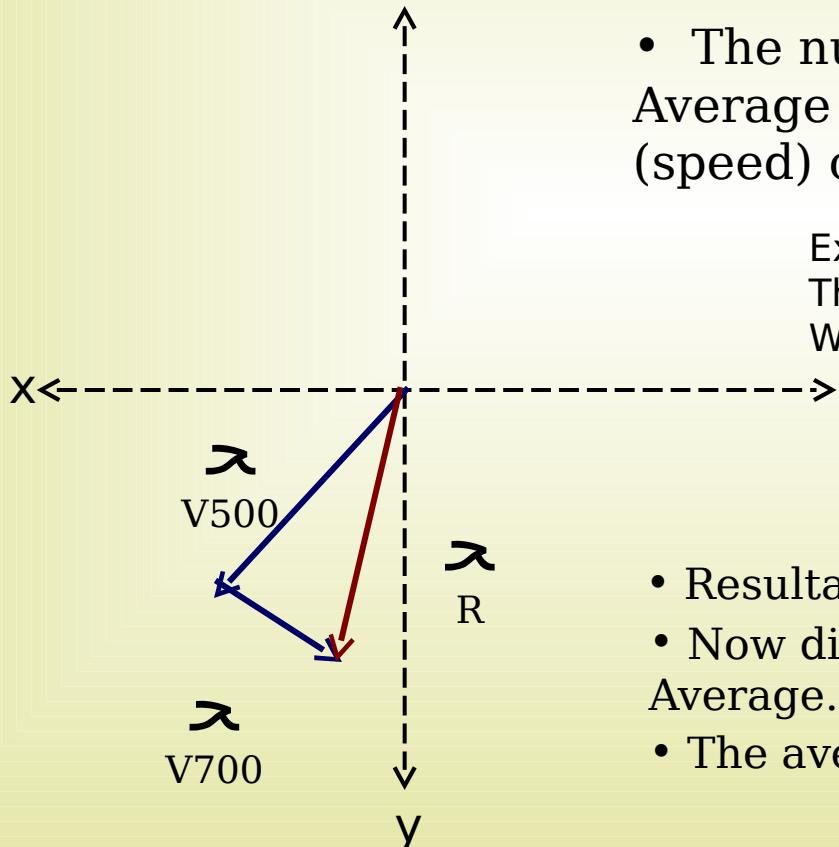
Ex. - A parcel of air is moving from 270 at 20 Knots. Added forces are from 360 at 30 knots.

VECTOR OPERATIONS.

Vector Addition

Addition – Utilize graphical “head-to-tail” method.

Meteorological Uses – Average Wind for a Layer



- The number of levels added to compute the Average wind for a layer divides the magnitude (speed) of the resultant wind – $(V1 + V2)/2$.

Ex. – The 700mb wind is 320 at 20.
The 500mb wind is 060 at 30.
What is the average wind?

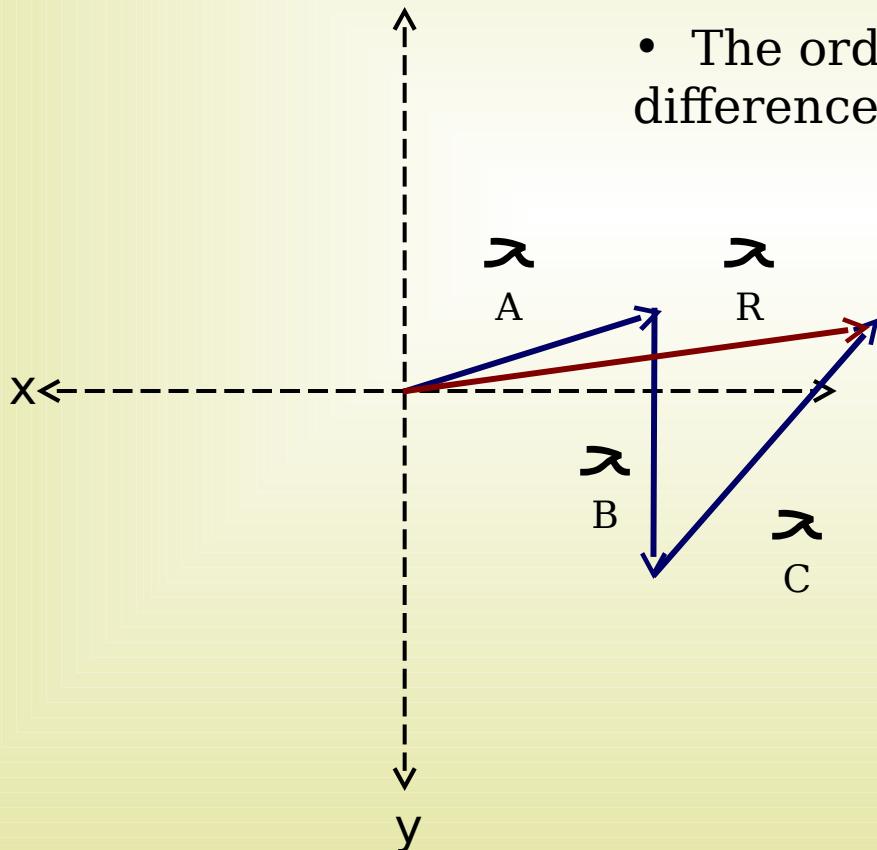
- Resultant vector is 210 at 34 knots.
- Now divide resultant speed by 2 to determine Average.
- The average wind is from 030 at 17 knots.

VECTOR OPERATIONS.

Vector Operations

Addition - Utilize graphical “head-to-tail” method.

Addition of 3 or more layers



- The order of addition does not make a difference.

$$\begin{aligned}\vec{A} &= 070 \text{ at } 15 \text{ kts} \\ \vec{B} &= 180 \text{ at } 15 \text{ kts} \\ \vec{C} &= 045 \text{ at } 20 \text{ kts}\end{aligned}$$

R Equals 080 at 28 knots

VECTOR OPERATIONS.

Vector Operations

Subtraction – Utilize graphical “Tail-to-tail” method

- Step #1 – Construct a x,y coordinate system.
- Step #2 – Select a scale and plot vector “A” and “B” to scale, with both tails at the origin.
- Step #4 – Draw the Resultant vector “R” from the head of the vector being subtracted to the head of the vector being subtracted from “A” ($A - B = R$).

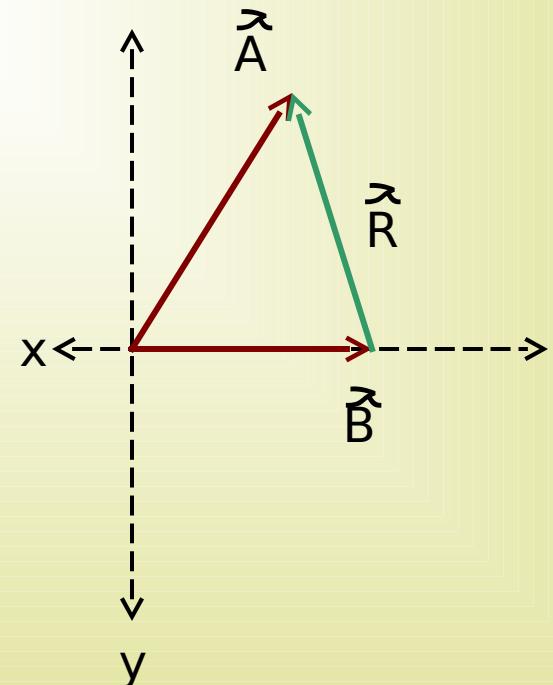
NOTE: The order of subtraction DOES make a difference

$$(A - B \neq B - A)$$

Meteorological

Uses Wind Shear.

- Cirrus Blowoff.



VECTOR OPERATIONS.

Vector Operations

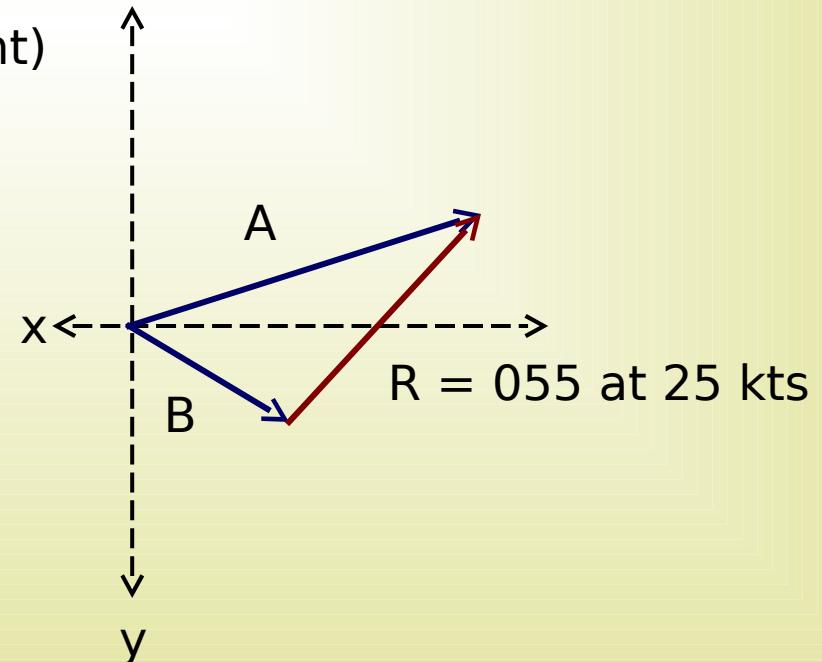
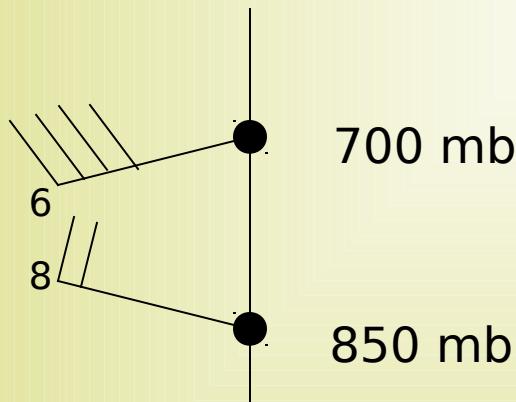
Subtraction – Utilize graphical “Tail-to-tail” method

NOTE: The order of subtraction DOES make a difference
 $(A - B \neq B - A)$

Meteorological Uses – Wind Shear.

- Change of wind speed and/or direction in the vertical or horizontal.

700mb - 850mb = Shear (resultant)



VECTOR OPERATIONS.

Vector Operations

Subtraction – Utilize graphical “Tail-to-tail” method

NOTE: The order of subtraction DOES make a difference
 $(A - B \neq B - A)$

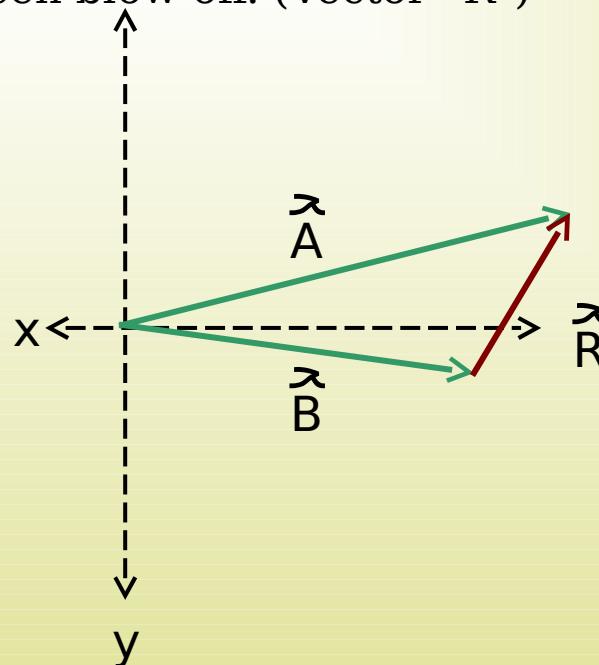
Meteorological Uses - Cirrus Blowoff.

- Wind flow aloft minus storm cell movement.
 - Cirrus starts at the origin and is blown off by the upper-level wind flow. (Vector “A”)
 - At the same time, the storm cell is moving. (Vector “B”)
 - It appears as if the cirrus has been blow off. (Vector “R”)

\vec{A} = Winds aloft
from 240 at 30 kts

\vec{B} = Cell Movement
towards 100 at 20 kts

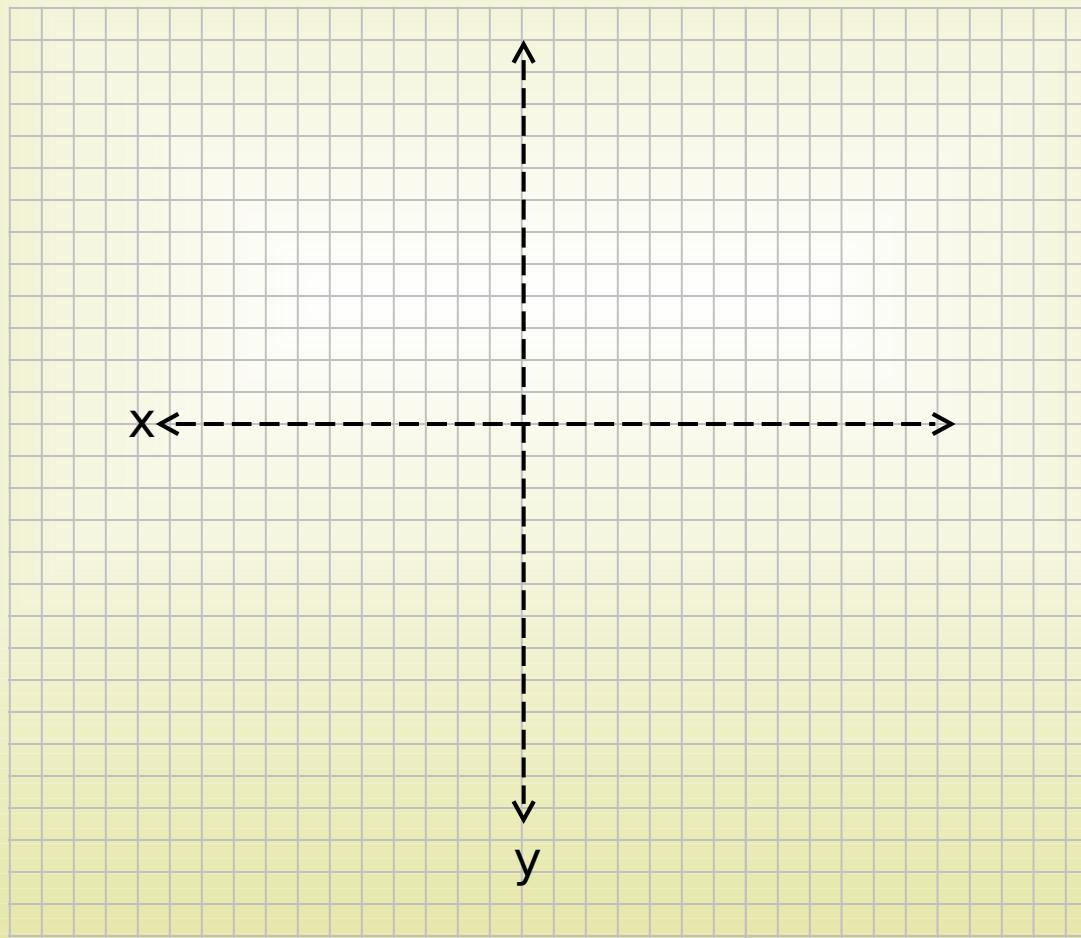
\vec{R} = Cirrus Blowoff
 $(A - B)$ 020 at 19.5 kts



VECTOR OPERATIONS.

Example #1

1. Find $A + B$ for the following. Express answer as a vector.
 - a. $A = 030^\circ/50$, $B = 150^\circ/25$
 - b. $A = 270^\circ/30$, $B = 345^\circ/60$

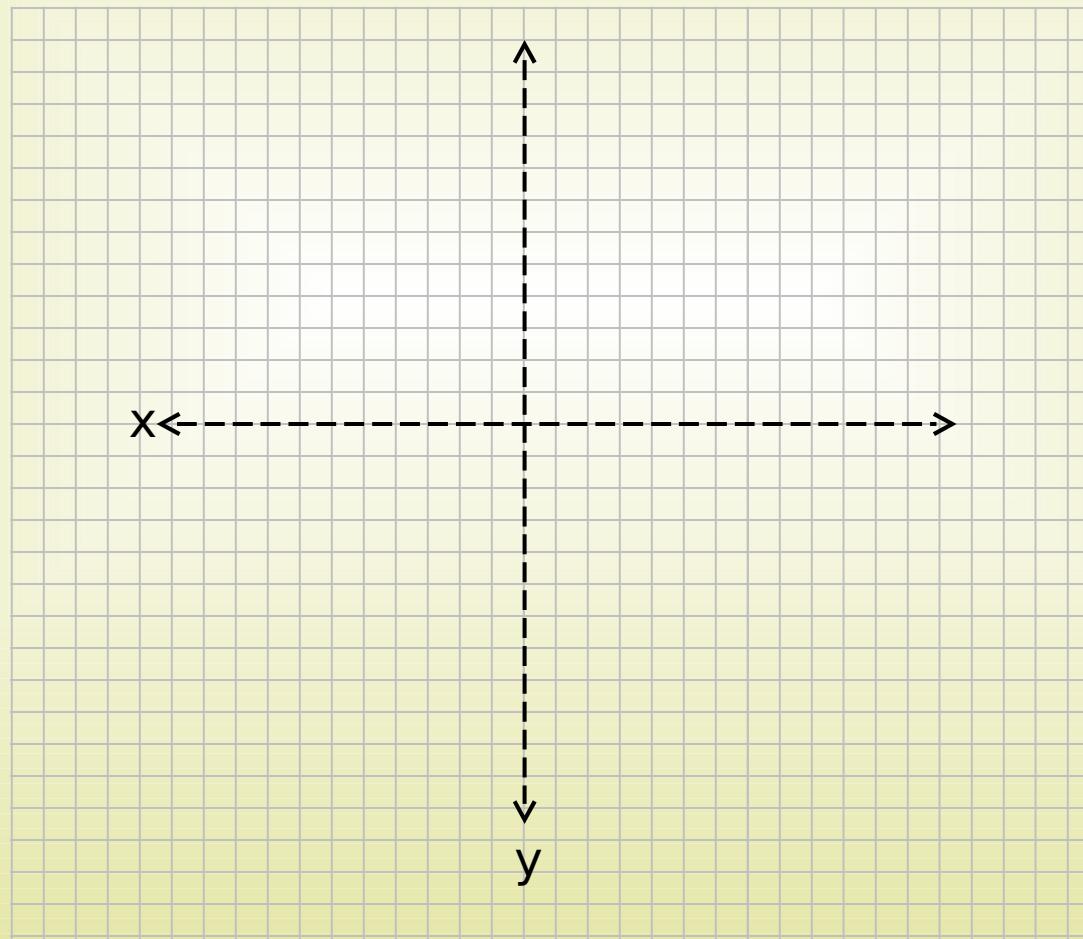


Scale: Each square represent 5 knots.

VECTOR OPERATIONS.

Example #2

1. Find the vertical wind shear between the 850 and 700mb levels if the 850mb wind equals 27020, and the 700mb equals 18020. Express as a vector.



Scale: Each square represents 5 knots.

VECTOR OPERATIONS.

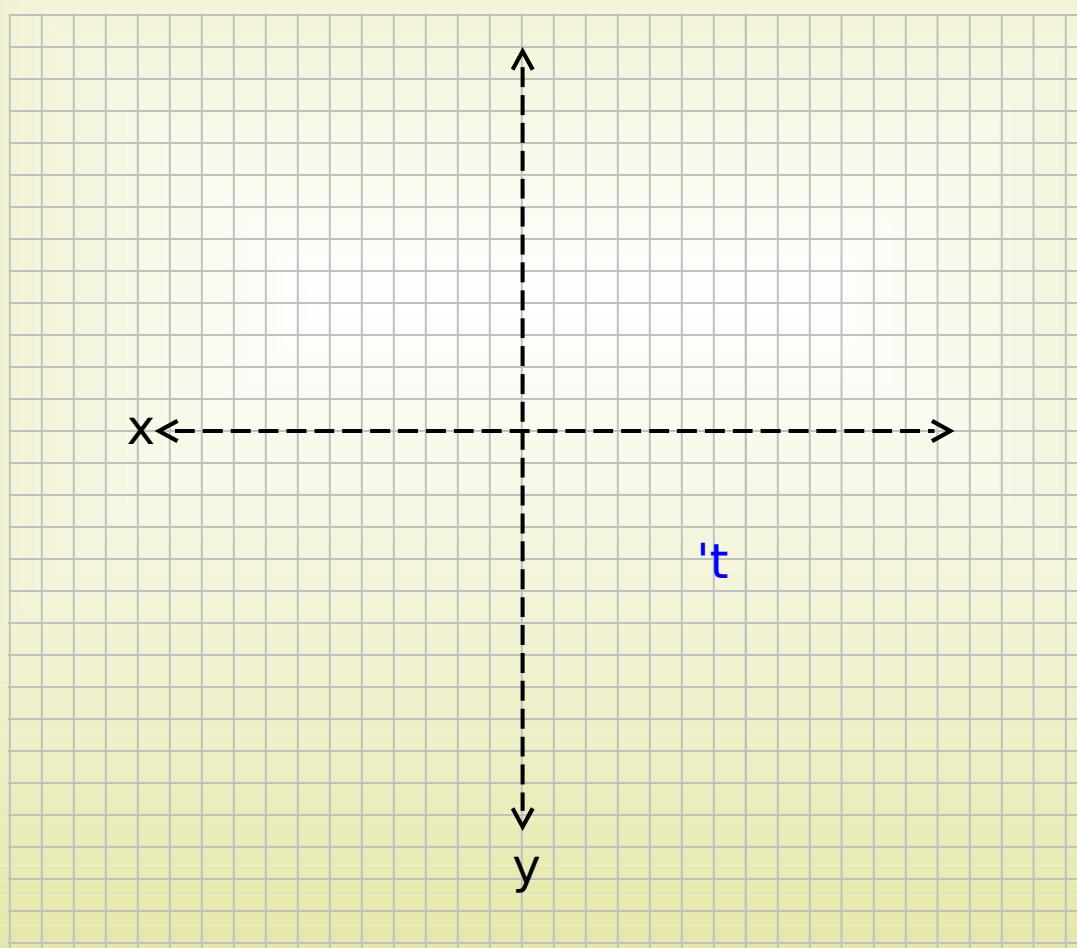
Example #3

1. Add the following vectors.

$$A = 09010$$

$$B = 14515$$

$$C = 30015$$

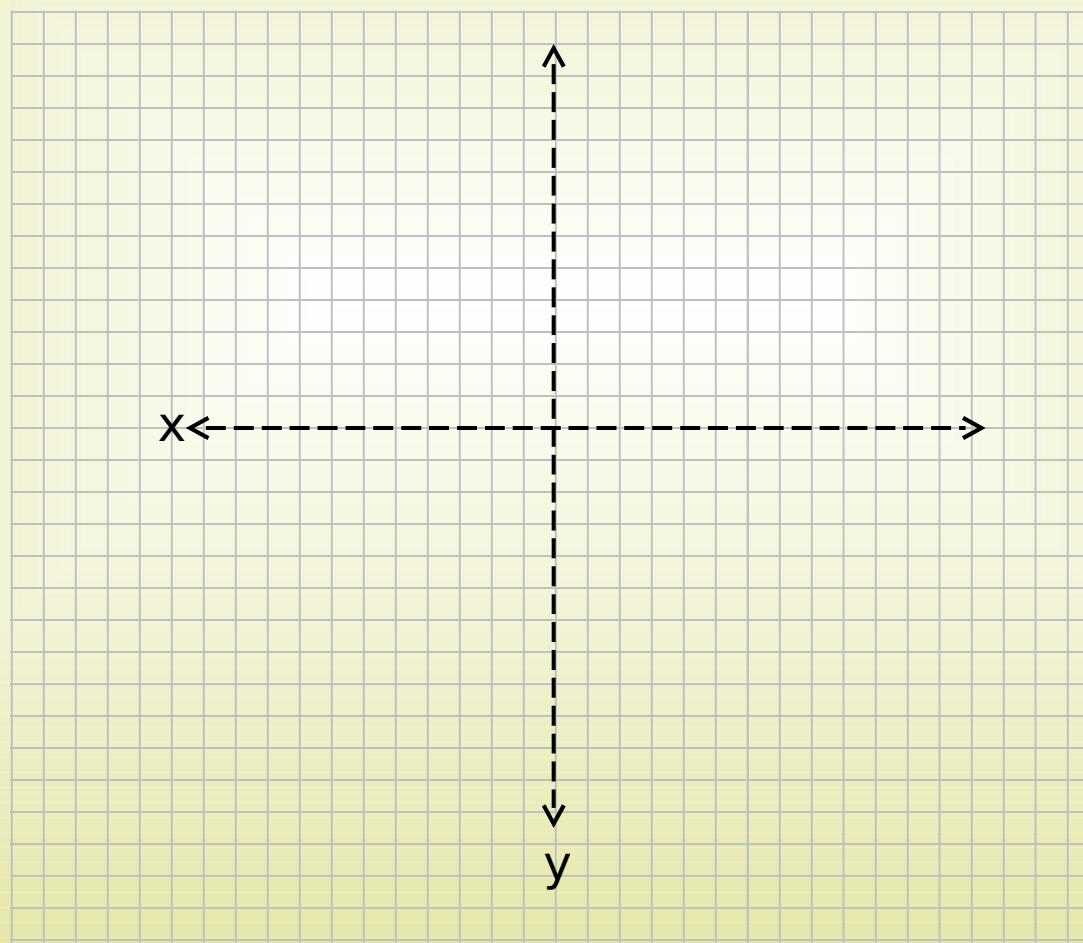


Scale: Each square represent 5 knots.

VECTOR OPERATIONS.

Example #4

1. Calculate the direction and speed of the cirrus blow-off for a thunderstorm if the prevailing wind is from 270 at 50 kts and the movement of the thunderstorm is toward 360 at 30 kts.



Scale: Each square represents 5 knots.

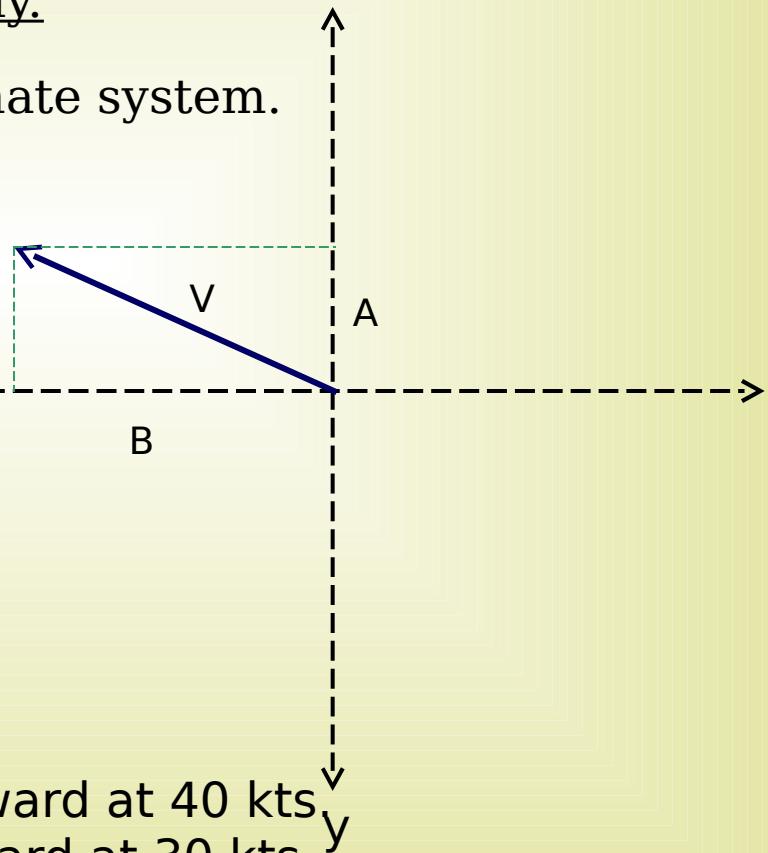
Vector Components.

Computing Components of Vectors

Component: The portion of a vector along a given coordinate system.

Determining vector components graphically.

- Step #1 - Draw a navigational coordinate system.
- Step #2 - Determine scale.
- Step #3 - Plot vector from origin.
- Step #4 - Drop a line from the head of the vector to each axis.
- Step #5 - Measure magnitude of each component.
- Step #6 - Determine direction of each component.



Component A = Northward at 40 kts
Component B = Westward at 30 kts.

Scale
1/4" is 10 kts

Vector Components.

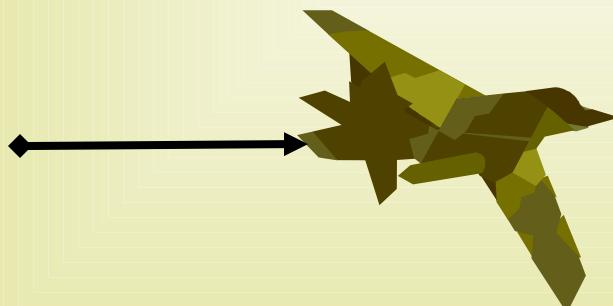
Computing Components of Vectors

Component: The portion of a vector along a given coordinate system.

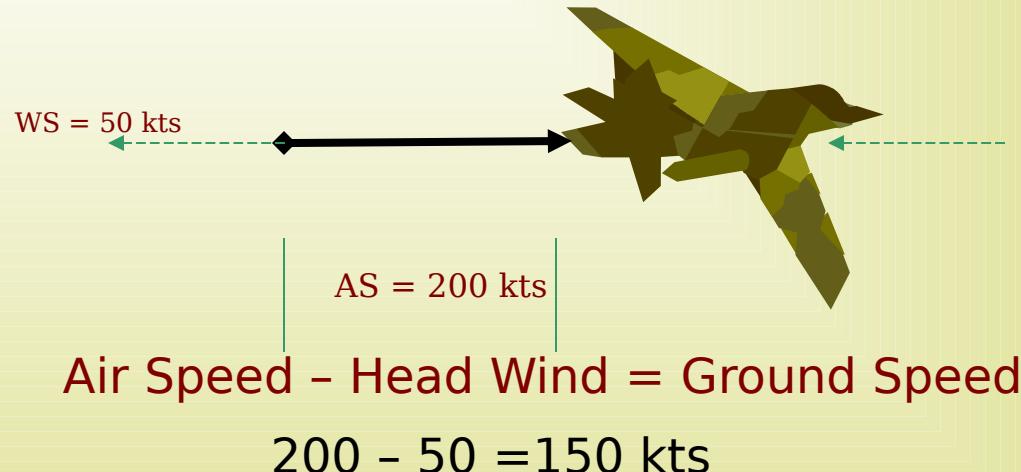
Commonly used terms with vector components:

- Air Speed – The speed at which an aircraft is flying relative to the wind.
- Ground Speed – The speed at which the aircraft is flying over, or relative to the ground.
- Head Wind – Component of the wind vector that is parallel to the aircraft's direction of motion. Opposed aircraft motion decreasing ground speed.

No Winds
Air Speed (AS) = Ground Speed (GS)



$$WS = 50 \text{ kts} \quad GS = 150 \text{ kts} \quad AS = 200 \text{ kts}$$



Vector Components.

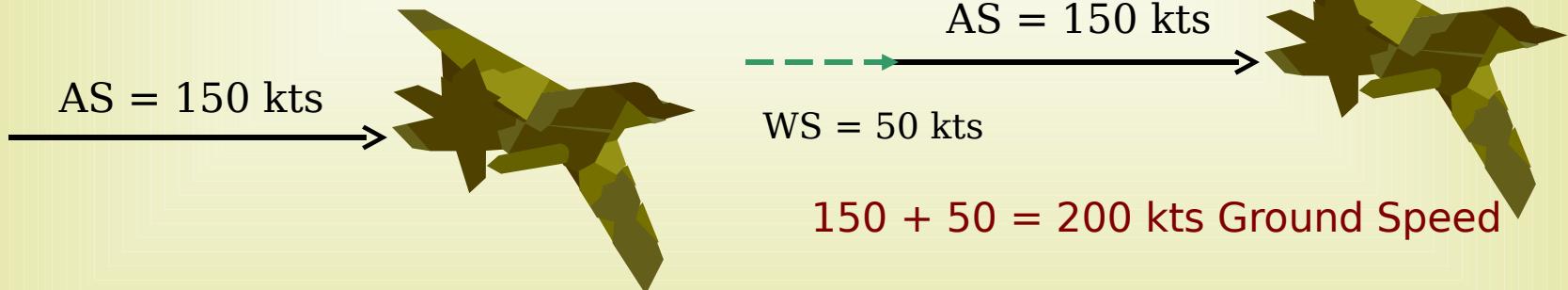
Computing Components of Vectors

Component: The portion of a vector along a given coordinate system.

Commonly used terms with vector components:

- **Tail Wind** – Component of the Wind vector that is parallel to the aircraft's direction of motion. Assists aircraft motion resulting in increased ground speed.

Air Speed + Tail Wind = Ground Speed



Vector Components.

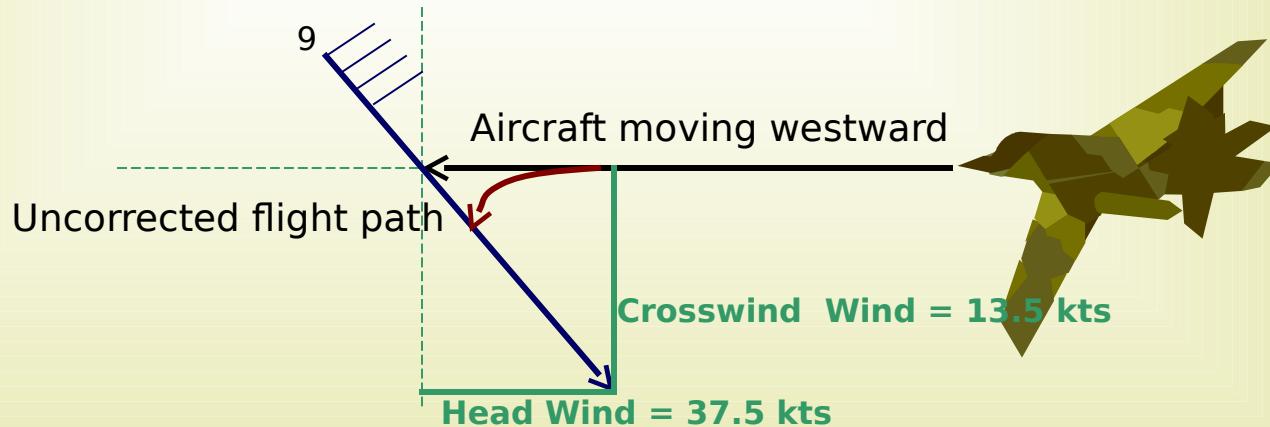
Computing Components of Vectors

Component: The portion of a vector along a given coordinate system.

Commonly used terms with vector components:

- **Crosswind** – Component of the wind perpendicular to aircraft's flight path. Requires change of aircraft heading in order to maintain desired course.

To determine the crosswind, use steps for determining vector components.



- **Runway Crosswind** – Component of the wind perpendicular to aircraft's flight path during take-off or landing. May require a change of runway for safe flight operations.

Vector Components.

Computing Components of Vectors

Component: The portion of a vector along a given coordinate system.

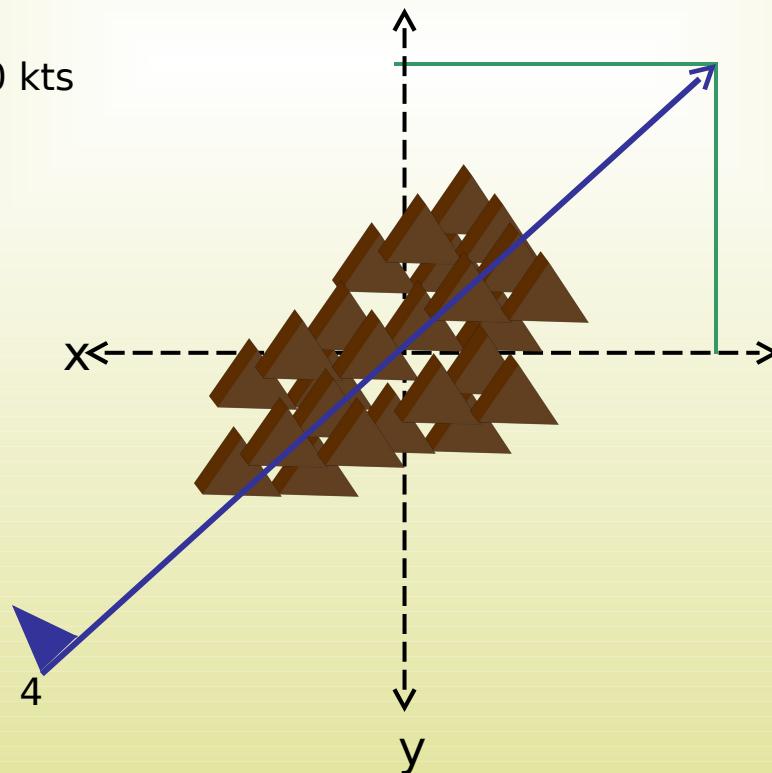
Commonly used terms with vector components:

- **Mountains** – Strength of the wind component perpendicular to the mountain range often has a definite impact on lee-side weather and downstream turbulence.

To determine the mountain crosswind, use steps for determining vector component

Observed Wind = 240 at 50 kts

Component Perpendicular to range = 090 at 30 kts



Questions?

